|   | 24 | P1 | for start to process of working out the unknown probabilities,   | Award for $P(R) + P(Y) = 0.48$ , may be seen in |
|---|----|----|--|---|
| 1 |    |    | eg 1 - 0.32 - 0.20 (= 0.48)  | table   |
|   |    |    | or assigning probabilities as $5x$ and $x$   |   |
|   |    |    | or process to work out the number of blue or green counters,   |   |
|   |    |    | eg 0.32 × 300 (= 96) or 0.20 × 300 (= 60) or 0.52 × 300 (= 156)  |   |
|   |    |    |  |   |
|   |    | D1 | Commence to Control of the control iller   |   |
|   |    | P1 | for process to find the probability,<br>eg $5x + x = \text{``}0.48\text{''} \text{ or '`}0.48\text{''} + 6 (= 0.08)$ |   |
|   |    |    | or process to find the number of red or yellow counters,   |   |
|   |    |    | eg 300 — "96" — "60" or 300 × "0.48"   |   |
|   |    |    | - C  |   |
|   |    |    |  |   |
|   |    | A1 | cao  |   |
|   |    |    |  |   |

|   | 0.78 | P1 | for using 0.75 or 0.25 in a relevant product,  | Allow different letters   |
|---|------|----|--|---|
| 2 |      |    | eg $0.75 \times x$ or $0.25 \times y$  | Could work with fractions   |
|   |      | P1 | for using two products to form an equation, eg $0.75x + 0.25y = 0.36$                                  |   |
|   |      | P1 | for a correct equation in one variable,<br>eg $0.75(1-p) + 0.25p = 0.36$ or $0.75f + 0.25(1-f) = 0.36$ | Could set up an equation for pass $\times$ pass $+$ fail $\times$ fail $=$ 0.64 |
|   |      | A1 | oe   | Accept 78% or any equivalent fraction,<br>39 156                                |
|   |      |    |  | $eg \frac{55}{50}, \frac{150}{200}$   |

| 3 | $\frac{11}{21}$ | P1 | for any product of 3 probabilities of the form $\frac{a}{9} \times \frac{b}{8} \times \frac{c}{7}$ where $a < 9, b < 8, c < 7$   | May see fraction with denominator 504  |
|---|-----------------|----|--|--|
|   |                 |    |  | Students who indicate they are using the approach $P(\text{even}) = 1 - P(\text{odd})$ should be given credit as appropriate |
|   |                 | P1 | for a product of 3 probabilities giving an even sum,<br>eg. E,E,E = $\frac{4}{9} \times \frac{3}{8} \times \frac{2}{7}$ or E,O,O = $\frac{4}{9} \times \frac{5}{8} \times \frac{4}{7}$   |  |
|   |                 | P1 | for summing the product of at least three correct triples, eg (E,E,E + E,O,O + O,O,E =) $\frac{4}{9} \times \frac{3}{8} \times \frac{2}{7} + \frac{4}{9} \times \frac{5}{8} \times \frac{4}{7} + \frac{5}{9} \times \frac{4}{8} \times \frac{4}{7} \text{ OR } 3(\frac{4}{9} \times \frac{5}{8} \times \frac{4}{7})$ |  |
|   |                 | A1 | for $\frac{11}{21}$ oe  SCB1 for answer of $\frac{364}{729}$ (replacement)   | Accept any equivalent fraction, decimal form 0.52(38) or percentage form 52(.38)%  |

| 4 | (a) | 1  | M1 | for method to find probability of getting a score of 5,       |   |
|---|-----|----|----|---|---|
| 4 |     | 16 |    | eg $\frac{10}{6+8+9+7+10} = (=\frac{10}{40})$ oe              |   |
|   |     |    | A1 | for $\frac{1}{16}$ oe   | Accept any equivalent fraction, decimal form 0.06(25) or 0.063, percentage form 6(.25)% or 6.3% |
|   | (b) | 15 | M1 | for method to find the proportion of 1s, eg $\frac{6}{40}$ oe | Ignore subsequent incorrect attempts to write the correct answer in a different form.           |
|   |     |    | A1 | cao   |   |

| _ | 62  | P1 | for process to find a probability of 2 cards of different colours,  | May see fraction with denominator 110   |
|---|-----|----|---|---|
| 5 | 110 |    | $   \text{ eg } \frac{3}{11} \times \frac{7}{10} \text{ or } \frac{3}{11} \times \frac{1}{10} \text{ or } \frac{7}{11} \times \frac{3}{10} \text{ or } \frac{7}{11} \times \frac{1}{10} \text{ or } \frac{1}{11} \times \frac{3}{10} \text{ or } \frac{1}{11} \times \frac{7}{10} \text{ oe } $ |   |
|   |     |    | or $\frac{3}{11} \times \frac{8}{10}$ oe or $\frac{7}{11} \times \frac{4}{10}$ oe or $\frac{1}{11} \times \frac{10}{10}$ oe   |   |
|   |     | P1 | for a complete process,   |   |
|   |     |    | $ \text{eg } \frac{3}{11} \times \frac{7}{10} + \frac{3}{11} \times \frac{1}{10} + \frac{7}{11} \times \frac{3}{10} + \frac{7}{11} \times \frac{1}{10} + \frac{1}{11} \times \frac{3}{10} + \frac{1}{11} \times \frac{7}{10} \text{ oe }                                  $                     |   |
|   |     |    | or $\frac{3}{11} \times \frac{8}{10} + \frac{7}{11} \times \frac{4}{10} + \frac{1}{11} \times \frac{10}{10}$ oe   |   |
|   |     | A1 | $ \operatorname{for} \frac{62}{110} $ oe  | Accept equivalent fraction, decimal form 0.56(36) or percentage form 56(.36)% |
|   |     |    | OR  |   |
|   |     | P1 | for process to find a probability of 2 cards of the same colour, eg $\frac{3}{11} \times \frac{2}{10}$ or $\frac{7}{11} \times \frac{6}{10}$ or $\frac{1}{11} \times \frac{0}{10}$ oe   |   |
|   |     | P1 | for a complete process, eg $1 - \frac{3}{11} \times \frac{2}{10} - \frac{7}{11} \times \frac{6}{10} \left( -\frac{1}{11} \times \frac{0}{10} \right)$ oe  |   |
|   |     | A1 | for $\frac{62}{110}$ oe   | Accept equivalent fraction, decimal form 0.56(36) or percentage form 56(.36)% |
|   |     |    | SC B1 for answer of $\frac{62}{121}$ (replacement)  |   |
|   |     |    |   |   |

| 6 | (a) | 0.7        | B1 | for 0.7 on the first branch           | Accept equivalent fractions or percentages for probabilities |
|---|-----|------------|----|---------------------------------------|--|
|   |     | 0.65, 0.65 | В1 | for 0.65, 0.65 on the second branches | probabilities  |
|   | (b) | 0.105      | M1 | for 0.3 × 0.35                        |  |
|   |     |            | A1 | oe                                    |  |

| 7 | 16 | P1 | for Prob(R or G) = $1 - 0.4 = 0.6$ )   |   |
|---|----|----|--|---|
|   |    | P1 | or for (number of red or green counters) = $50 - 0.4 \times 50$ (= 30) or for use of ratio, eg [probability] $\times \frac{8}{15}$ (= 0.32) or [number of counters] $\times \frac{8}{15}$ for a complete process to find number of green counters, eg $(1 - 0.4) \times \frac{8}{15} \times 50$ or for $\frac{16}{50}$ | [probability] may be 0.4 or 0.6<br>[number of counters] may be 20 or 50 |
|   |    | A1 | cao  |   |

| 8 (a) | 225<br>3600 | P1 | for process to use relative frequency for landing on a 6, eg $\frac{15}{60}$ oe   |  |
|-------|-------------|----|---|--|
|       | 3000        | P1 | for $\frac{15}{60} \times \frac{15}{60}$ oe, eg $\frac{1}{4} \times \frac{1}{4}$  |  |
|       |             | A1 | for $\frac{225}{3600}$ oe, eg $\frac{1}{16}$  | Accept any equivalent fraction, decimal form 0.06(25) or 0.062 or 0.063, percentage form 6(.25)% or 6.2% or 6.3% Ignore subsequent attempts to write the correct answer in a different form. |
| (b)   | Explanation | C1 | for a correct explanation Acceptable examples $n$ must be greater than 60 She must do it more times than in (a) $n$ must be bigger, eg 100              |  |
|       |             |    | Not acceptable examples If you increase the number of results, you increase the accuracy <i>n</i> must be bigger <i>n</i> is an integer <i>n</i> is 100 |  |

| 9 | $\frac{5x^2 - 23x + 50}{9x^2 - 3x}$ | P1 | for using $y = 3x$ or $x = \frac{1}{3}v$ to obtain an expression for a probability in one variable   | This may be awarded at any time         |
|---|-------------------------------------|----|--|---|
|   |                                     | P1 | for a correct second probability $\operatorname{eg} \frac{x-1}{y-1} \operatorname{or} \frac{x-1}{3x-1} \operatorname{or} \frac{4}{y-1} \operatorname{or} \frac{4}{3x-1} \operatorname{or} \frac{y-x-6}{y-1} \operatorname{or} \frac{2x-6}{3x-1}$   |   |
|   |                                     | P1 | for forming a correct product  |   |
|   |                                     |    | $\operatorname{eg} \frac{x}{y} \times \frac{x-1}{y-1} \operatorname{or} \frac{x}{3x} \times \frac{x-1}{3x-1}$  |   |
|   |                                     |    | or $\frac{5}{y} \times \frac{4}{y-1}$ or $\frac{5}{3x} \times \frac{4}{3x-1}$  |   |
|   |                                     |    | or $\frac{y-x-5}{y} \times \frac{y-x-6}{y-1}$ or $\frac{2x-5}{3x} \times \frac{2x-6}{3x-1}$  |   |
|   |                                     | P1 | for adding the 3 correct probabilities<br>eg $\frac{x}{y} \times \frac{x-1}{y-1} + \frac{5}{y} \times \frac{4}{y-1} + \frac{y-x-5}{y} \times \frac{y-x-6}{y-1}$<br>or<br>$\frac{x}{x} \times \frac{x-1}{3x-1} + \frac{5}{3x} \times \frac{4}{3x-1} + \frac{2x-5}{3x} \times \frac{2x-6}{3x-1}$ | Can be seen after processing of algebra |
|   |                                     | A1 | $ \begin{array}{cccccccccccccccccccccccccccccccccccc$  |   |